Adaptive Just-in-time Value Class Optimization

Transparent Data Structure Inlining for Fast Execution

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ABSTRACT
The performance of value classes is highly dependent on how they are represented in the virtual machine. Value class instances are immutable, have no identity, and can only refer to other value classes or primitives and since they should be very lightweight and fast, it is important to optimize them well. In this paper we present a technique to detect and compress commonly occurring patterns of value class usage to improve memory usage and performance. Micro-benchmarks show two to ten-fold speedup of a small prototypical implementation over the implementation of value classes in other object-oriented language implementations.

Categories and Subject Descriptors
D.3.3 [Language Constructs and Features]: Data types and structures, Dynamic storage management; D.3.4 [Processors]: Code generation, Compilers

Keywords
Meta-tracing, JIT, Data Structure Optimization, Value Classes

1. INTRODUCTION
Objects are at the heart of object-oriented languages and the choice of how to represent them in memory is crucial for the performance of a language implementation [3, 27]. The standard way of representing objects involves an indirectness for references to other objects, e.g. by using direct pointers or object tables. Typical best practices of object-oriented modeling and design—such as delegation or the composite design pattern—have an influence on performance with such representations. Every additional indirection between delegators and delegates or composites and their parts has the overhead of a new object. This includes memory consumption, but also execution time to navigate the referenced objects.

In this paper we propose an object layout that stores nested object groups in a compacted, linearized fashion. To simplify the problem, we restrict ourselves to optimizing value classes [2]. Value classes are immutable classes without identity that only store other value classes or primitive data. Value classes are available in Java [31], Scala [28], and .Net [25], to name a few. Composite structures involving value classes have certain usage patterns. This is obvious in linked lists (a single list element probably references another list element and so forth) or trees (a tree node references a number of other nodes or a value). Data structures with such patterns can be transformed into lower-level structures more suitable to the machine model. While simple variants of such patterns can be statically inferred, many become apparent only at run-time. In particular, recursive structures often exhibit patterns that are opaque to static inference, e.g. while a tree apparently may have sub-nodes, it is statically unknown whether trees are used as deep trees or rather flat ones, or which kind of values are stored in the tree in practice. However, each case could be optimized differently. Hence our optimization approach works at run-time in conjunction with a just-in-time (jit) compiler.

In this paper, we describe the following contributions:

- We propose an approach for finding patterns in value class usage at run-time.
- We present a compressed layout for value classes that makes use of the patterns to store value classes more efficiently.
- We report on the performance of micro-benchmarks for a small prototype language.

The paper is structured as follows: section 2 gives brief introductions to tracing jit compilers [6]. In section 3, we present our approach to just-in-time optimization of data structures. A proof-of-concept implementation is briefly presented in section 4 and its performance is evaluated in section 5. Our approach is put into context in section 6 and we conclude in section 7.

2. TRACING JUST-IN-TIME COMPILERS
Just-in-time (jit) compilation has become a mainstream technique for, among other reasons, speeding up the execution of programs at run-time. After its first application to Lisp in the 1960s, many other language implementations have benefitted from jit compilers—from APL, Fortran, or Smalltalk and Self [1] to today’s popular languages such as Java [29] or JavaScript [24].

One approach to writing jit compilers is using tracing. A tracing jit compiler records the steps an interpreter takes to obtain an instruction sequence called trace and then uses this trace instead of the interpreter to execute the same part of that program [26] at higher speed. Tracing produces specialized instruction sequences, e.g. for one path in if–then–else constructs; missed branches still use the interpreter. Tracing jit compilers have been successfully used for optimizing native code [4] and also for efficiently executing object-oriented programs [19].
3. OPTIMIZATION APPROACH

Our optimization detects common patterns of how instances of value classes (value objects for short) reference each other. It then introduces short forms for these patterns, which we call shapes, that make it possible to represent these patterns more efficiently in memory. This physical representation of the data structures is separated from the interface visible to programmers.

A straightforward value object representation would be a chunk of memory that stores a pointer to the class of the value object, followed by its contents that typically consist of pointers to all the fields of that value object. We call the contents the storage of the value object. The class describes the storage, e.g. how many fields there are and how they are to be interpreted. This representation corresponds very closely to the programmers’ view on value classes.

In our approach, the storage area remains, but the pointer to the class is replaced by a pointer to the shape. As with the regular representation, the shape determines the class of the value object and hence the meaning of its contents. Two examples for this separation can be found in Figure 1. For every value class there is a default shape that has no additional information compared with directly storing the class. If the default shape was always used, the representation would be completely equivalent to the straightforward one.

The difference from the straightforward representation is that a shape does not necessarily describe only the class of the value object. Rather, a shape can additionally describe the shape of referenced value objects, recursively. If a referenced value object’s shape is not specified in the referencing object’s shape, it is stored as a reference in the storage. If the shape is specified, that value object’s content is inlined into the referencing value object’s storage. That way, referenced values are stored compactly, i.e. in spatial proximity without overhead such as headers or a pointer between them, and hence with less memory consumption compared to storage without compaction. This process can be applied recursively.

To actually save memory, a shape has to be shared by significant number of value objects. Indeed, if every shape were used by only one object, the memory use would not be improved. Therefore, a new shape should only be introduced after run-time profiling ensures that it occurs often enough.

To understand the rest of the system, we now need to look at (a) how structure patterns are recognized, (b) how the construction of values ensures the proper usage of shapes, and (c) how the field reading of inlined fields is implemented.

3.1 Shapes and their recognition

A shape (in all figures) describes the abstract, structural representation of composite value objects and is shared between all identically structured value objects of the same value class, denoted by its name.

Shapes can be recursive; they consist of sub-shapes for each field in a value object’s storage. A special, non-recursive type of shapes denotes unaltered access to object content (direct access, in all figures) and termination of shape recursion. Value objects with these shapes are treated as black boxes, e.g. scalar data or unoptimized objects that are stored directly. This is depicted in the bottom part of Figure 1; all three nodes in the list share the same shape, which denotes that each node consists of two references with direct access shapes. The same holds for the nodes of the tree in that figure, but with three references.

Storing the shape of value objects may seem redundant given that the shape matches what it tries to describe. This only holds as long as no optimization has taken place. In this case, a value object’s shape is the default shape of its value class and solely consist of direct access sub-shapes. The shapes in Figure 1 are the default shapes for their value classes.

Further, a mapping of replacement options for inlining (the transformation rules), and profiling data built up during object creation to aid the creation of new transformation rules (the history) are supplementary structures that we use to aid the inlining process.

3.1.1 History

The immutability of value objects demands that all to-be-referenced value objects will constitute the content of a new value object have already been constructed beforehand. Hence, their shapes will be available at construction time and we can count occurrences of sub-shapes at specific positions in the value object. That way, we obtain a histogram of all possible shapes a referenced value object can have. In Figure 2, e.g. for shape s1 at position 1, the shape s1 itself has been encountered 17 times as sub-shape, while shape s2 has been encountered 3 times as sub-shape in that position.

When a certain threshold of encounters has been reached, we generate a new transformation rule.

3.1.2 Transformation rules and recognition

The transformation rules are mappings Shape×Position×Shape → Shape that drive the inlining process. When constructing a new value object, they are consulted by the inlining algorithm. These mappings can be specified prior to program execution or inferred dynamically based on shape history.

Upon value object creation, just after updating the shape history, we check whether the sub-shape counters hit a certain threshold, and if so, proceed to create a new shape that combines the value object’s current shape with the sub-shape that hit the threshold. In this new shape, we replace the direct access sub-shape at the position of the threshold hit with the sub-shape found in the history entry. The position of the hit, the sub-shape at that position, and the newly created shape are then recorded as new rule in the transformations table. Considering Figure 2 as example, shape s2 would be the result of turning the history entry (s1, 1, s1, 17) into the transformation rule (s1, 1, s1, 17) → s2. The structure of shape s2 is the structure of shape s1 but with another s1 structure in the final position.

We call the process of recording the shape history and inferring transformation rules shape recognition.

3.2 Compaction though inlining

Since value objects are immutable, compaction is required only when creating new ones. With this premise, our optimization technique works by inlining the to-be-referenced value objects into the to-be-created value object upon its creation.

3.2.1 Inlining

Meta-tracing takes this approach one step further by observing the execution of the interpreter instead of the execution of the application program. Hence, a resulting trace is not specific to a particular application but the underlying interpreter [10, 13]. Therefore, it is not necessary for a language implementer to program a optimized language-specific JIT compiler but rather to provide a straightforward language-specific interpreter in RPython, a subset of Python that allows type inference. Hints to the meta-tracing JIT enable fine-tuning of the resulting JIT compiler [9]. RPython’s tracing JIT also contains a very powerful escape analysis [7], which is an important building block for the optimization described in this paper.
When a new value object is created, we handle the default shape \( s \) for the type and the value object’s new content \( c \) as specified in the algorithm in Figure 4. We iterate over the given new content and for each to-be-referenced value object \( o_i \) at position \( i \) and its sub-shape \( s_i \), we look up a replacement shape in the transformations table. If the table contains a mapping, the replacement shape \( s' \) is assumed as the shape of the to-be-created value object. At that point, the storage of the current value object \( c_i \) is spliced into the current content \( c \) instead of the current value object \( c_i \) itself; the value object \( c_i \) is now inlined. After a successful inlining, the new shape \( s' \) becomes the to-be-created value object’s shape \( s \) and the current content is reiterated from start to allow for possible other transformations due to the shape change. That way, transition chains are possible that may quickly lead to shapes of deeply nested structures. Once no further transitions are found, the value object’s shape \( s \) and the current content \( c \) are returned as the shape and storage of the new value object.

The effect of this process is shown simplified with the example in Figure 3: creating a new node consisting of “1” and a rest list as in the figure. We start with a list of “1” and the rest list as initial content for the new value object and shape \( s_1 \) as the initial default shape. We iterate over the list and encounter “1” at position 0. For this example, we assume that the transformation table does not contain a mapping for “1” at position 0, thus \( s' \) will be \( s \) and we continue with the next position. At position 1, we find the rest list with the sub-shape \( s_2 \) as the initial default shape. In the transformation table, the entry for \( (s_1, 1, s_2) \) holds a replacement shape, \( s_3 \). Thus, we inline the current value object’s storage into the current content as \( s' \), which now has three elements. Note that it is not the shape of the rest list \( s_1 \) that is changed but rather the shape \( s \) of the to-be-created value object. The content, now \( c \), is reiterated but no further transformations are found. The resulting value object is that to the right in Figure 3.

The shape of thusly optimized value objects are themselves subject to the shape-recognition process and eventually, transition rules to more optimized shapes can be created in the default shapes for the value classes. Thus, more specific shapes are directly available for the inlining process. Value objects can be more directly transitioned into the most optimized shape compared to working off a long transition chain.

This inlining technique has two main advantages. First and foremost, inlined value objects take up less space than individual, inter-referenced value objects. But even more, the shape of a value object provides structural information in a manner the meta-tracing jit compiler can speculate on. This is crucial for optimizing the access to references of a value object.

### 3.3 Transparent field access

While optimization of data structures takes place during construction, we have to apply the reverse during deconstruction, i.e. when accessing a value object referenced by another. This is no longer trivial, as several (formerly referenced) value objects may have been inlined into their referencing value objects. Therefore, we construct new value objects whenever a reference is navigated, essentially reifying it. We use the information a value object’s shape provides to identify which parts of the value object’s storage comprise the value object to be reified. The structural information allows a direct mapping from the language view of the data structure to the actually stored elements. In Figure 5, the structural information in the shape of the leftmost list allow the reasoning that the first element of the storage is equivalent to the head of the language level node value object and the remaining three storage elements are equivalent to the tail of that value object, as recored in the shape. Hence the middle view in that figure; both the element “1” and the rest list have been reified. The same goes for the rightmost view.

Note that this reification is completely transparent to the programmers. Taking, e.g. the tail of a node value object or accessing the third element of a ternary tree repeatedly, the operations remain the same on the language level, no matter what is the inlining status of the value objects on the implementation level.

### 3.4 Benefits

With the inlining approach, fewer value objects need to be created for long living data structures, since the references to the now-inlined value objects are elided. Combining this with the reification and the shape recognition, more memory is saved the longer a program runs; the shapes will be tailored to fit the specific application running. That said, there may be cases where no memory can be saved, especially in programs that only work on primitive data, non-composite data structures, or with a high amount of sharing between data structures.
Figure 3: When creating a new node value object that should contain “1” and the list as shown, a new value object that merges the “1” with the “2” object and a different shape is created instead.

\begin{verbatim}
Input: s : Shape, c : [Object]
i ← 0
while i < |c| do
  o ← c_i
  s, c'(i) ← \text{transformations}_{i,i_c} \text{ or } s
  if s' \neq s then
    c' ← \{c_{i,i-1}, o_{\text{shape}}, c_{i+1,\ldots|c|}\}
    s ← s'
    // rewind over new storage:
    i ← 0, c ← c'
  else
    i ← i + 1
end
return s, o
\end{verbatim}

Figure 4: Merging composite objects based on shape

4. IMPLEMENTATION IN RPYTHON WITH A TRACING JIT COMPILER

We implemented our optimization approach in a simple execution model\footnote{available at https://bitbucket.org/krono/lamb}. It provides a λ-calculus with pattern matching as the sole control structure and is implemented as a direct application of the CJK-machine [17]. The only structured data types currently available are value classes. We used the RPython tool chain to incorporate its meta-tracing \texttt{jit} compiler [6]. The implementation has been carefully unit-tested during development to make sure that various complex substitutions and compactions work correctly.

The presence of the \texttt{jit} compiler is necessary to begin with, because the approach just presented, i.e. shape recognition, inlining, and reified reference access combined, does not yield a performance increase on its own. In fact, implementing the approach naïvely yields significantly worse performance than leaving it out altogether, due to the constant check of the transformation rules every time a new value object is created. Additionally, reading inlined fields of compacted value objects results in the allocation of intermediate data structures. This is of course not the case in the naïve representation.

To improve performance, the \texttt{jit} compiler needs to reduce the overhead of these operations. The first step is to treat the transformation tables as constant when a function is compiled. This allows the \texttt{jit} compiler to compile value object creation down to a series of type checks for the types of the referenced value objects. While the transformation tables are not constant per se, we instruct the \texttt{jit} compiler to treat them as such for all practical purposes.

Second, we have to avoid the otherwise necessary reification of referenced value objects when it is being read from a value object it has been inlined into. For that, the observation that most of these intermediate value objects are actually short-lived is crucial; most value objects are created just to be either immediately discarded or consumed in another, typically larger data structure. As a concrete example, typical linked list operations deconstruct the list they are working on. Hence, if the tail is read off a linked list node which has the tail inlined (as the transition from left to middle in Figure 5) and needs to be reified, that tail is usually soon deconstructed itself into its head and tail components (as the transition from middle to right in the same figure). This allows the tracing \texttt{jit} compiler to optimize the reading of fields that need reification. Since the value objects allocated when reifying a field are short-lived, the built-in escape analysis [8] will fully remove their allocation and thus remove the overhead of reification.

5. RESULTS

We report the performance of five micro-benchmarks, i.e. their execution time and their maximal memory consumption (resident set size). The benchmarks chosen are \texttt{append}, \texttt{filter}, \texttt{map}, and \texttt{reverse} on very long linked lists and the creation and complete prefix traversal of a binary tree. Due to the limited feature scope of our prototype, more sophisticated applications are currently not available for benchmarking.

In the left part of Figure 6, the execution time of all benchmarks is reported. Our implementation, labeled \texttt{prototype \texttt{a}}, is significantly faster—from two to ten times faster—for all but the tree benchmark, where our implementation is second to just the ahead-of-time (aat) compiled OCaml version. However, the other two RPython-based implementations are likewise significantly slower than expected; the Pycket interpreter uses the same CJK execution model as our implementation. It is possible that not the value class implementation but the interpreter style is responsible for most of the execution time. Nevertheless, our implementation is still significantly faster than both RPython-based implementations. For memory consumption, shown in the right part of Figure 6, our implementation always uses significantly less memory than the other implementations.

One key reason for our prototype’s performance is the interaction between escape analysis and the compacted storage. The benchmarks exhibit a certain usage pattern, in particular, the access to a list element is typically followed by inserting this element into a new list, with possibly processing it. The tracing \texttt{jit} compiler and its escape analysis can infer that no reification of the actual value object is necessary and, furthermore, that a certain number of such operations occur consecutively. Hence, operations can happen \texttt{en bloc}, e.g. for a list inlined \texttt{n} levels deep, reverse can operate in \texttt{n}-chunks of items.

Our approach makes use of three parameters that may influence performance:

**Maximum object size** Only value objects up to this size are considered for inlining. Setting this to to zero disables our optimization, setting it to a very high number might result in very large value object at runtime, which might be undesirable. We used a maximum size of \texttt{7} fields for our measurements.
Maximum shape depth. The number recursive shape occurrences per value object is bounded by this parameter. Setting this to a low value may not catch all optimizable object shapes, setting it to a very high number may lead to an excessive number of shapes at runtime should there be a lot of value objects with no fields at all. We used a maximum depth of 7 shapes for our measurements.

Substitution threshold. The threshold for transformation rule creation (as in section 3.1.2), when set to a zero or a very low value can lead to excessive transformation rule creation for value object combinations that are only rarely used. A very high number might inhibit the creation of such rules at all and practically disables our optimization. We used a threshold of 17 shape occurrences for our measurements. The results suggest that our approach is viable and warrants application to other programming languages.

Setup.

Hardware. The processor used was an Intel Xeon E5410 (Harpertown) clocked at 2.33 GHz with 2x6 MB cache; 16 GB of RAM were available. All runs are un-parallelized, hence the number of cores (four) was irrelevant to the experiment. Although virtualized on Xen, the machine was dedicated to the benchmarks.

Software. The machine ran Ubuntu 12.04.4 LTS with a 64 bit Linux 3.2.0. The benchmarking framework ReBench\(^3\) was used to carry out all execution of the benchmarks and collection of measurements. RPython as of revision 5a423327c96a served for translation.

 Compared Implementations. We included OCaml \[\textcolor{red}{\textsuperscript{3}}\], Racket \[\textcolor{red}{\textsuperscript{3}}\], Pycket \[\textcolor{red}{\textsuperscript{3}}\], and PyPy \[\textcolor{red}{\textsuperscript{3}}\] in the comparison. For all these, value classes or equivalent means supporting immutable data are available. OCaml provides a concept similar to value classes with its algebraic data types and its execution model bears similarities to our implementation. OCaml produces native binaries. Racket’s cons cells, structs and classes can act as value classes. Racket acts as virtual machine with hand-written \texttt{rr} compiler. Pycket \[\textcolor{red}{\textsuperscript{3}}\] is a RPython implementation of Racket and provides a meta-tracing \texttt{rr} compiler. PyPy is the RPython implementation of Python and has a meta-tracing \texttt{rr} compiler. While Python has no actual concept of value classes, we used regular classes without mutating them. PyPy is then able to handle them as value classes. We intended to also include the standard Python (CPython) but it was too slow and would have rendered the comparison meaningless.

Methodology. Every benchmark was run ten times uninterrupted at highest priority, in a new process. The execution time (\textit{total time}) was measured \textit{in-system} and, hence, does not include start-up; however, warm-up was not separated, so \texttt{rr} compiler execution time is included in the numbers. The maximal memory consumption (\textit{resident set size}) was measured \textit{out-of-system} and may hence include set-up costs. We report the arithmetic mean of the ten runs. The error was negligible. We provide all numbers in the appendix. Our benchmarking code and infrastructure are publicly available.\(^4\)

6. RELATED WORK

From a data structure optimization point of view, value classes are similar to \textit{algebraic data types} as found in languages in the ML family. Hence, optimizations done to this category of data structures are relevant to value classes, too.

Wimmer has proposed object inlining \[\textcolor{red}{\textsuperscript{37}}\] as a general data structure optimization for structured objects in Java. Superficially, this approach is similar to this work, yet object inlining is restricted to statically typed object oriented languages like Java, as the approach needs full knowledge of all class layouts until just before \texttt{rr} compilation. Moreover, object inlining is bound to create one “optimized path” per class.

Language-level optimization. The idea to improve data structures to gain execution speed was proposed especially to improve operations on linked lists in functional languages, e.g. by unrolling \[\textcolor{red}{\textsuperscript{32}}\]. Typically, those optimizations are restricted to linked lists of cons-cells.

One of the key effects in our optimization is avoiding to allocate intermediate data structures. In that respect, hash consing \[\textcolor{red}{\textsuperscript{16, 18, 23}}\], as used in functional languages for a long time, is related to this work. However, hash consing typically works at the language level using libraries, coding conventions, or source-to-source transformations. It is not adaptable at run-time.

Ahead-of-time optimization. Deforestation \[\textcolor{red}{\textsuperscript{21, 34, 36}}\] has the aim to eliminate intermediate data structures and is in this respect related to our approach. However, deforestation deliberately works through program transformation and does not incorporate dynamic usage information. It is typically only available to statically typed functional languages, such as ML.

Just-in-time compilers. Compiling to native code at run-time, i.e. \texttt{rr} compilation, is a prevalent and extensively studied technique, found in several different, but chiefly object-oriented, dynamically-typed languages \[\textcolor{red}{\textsuperscript{1}}\]. Prominent examples include the Smalltalk-80 bytecode-to-native-code compiler by Deutsch and Schifflman \[\textcolor{red}{\textsuperscript{15}}\], and the optimizing \texttt{rr} compiler of Self, with type specialization and speculative inlining \[\textcolor{red}{\textsuperscript{14}}\]. These concepts were later used in the HotSpot \texttt{rr} compiler \[\textcolor{red}{\textsuperscript{29}}\] for Java.

The prevalence of web browsers has made \texttt{rr} compilation an important topic for JavaScript implementations, e.g. the \texttt{int V8} JavaScript implementation \[\textcolor{red}{\textsuperscript{24}}\].

\textit{Nota bene}: The map transitions for hidden classes used in V8 \[\textcolor{red}{\textsuperscript{22}}\] and inspired by Self \[\textcolor{red}{\textsuperscript{14}}\], are in principle similar to our notion of transformation rules. As well as objects in V8 start with a default hidden class and follow map transitions to their most optimal hidden class, the transformation rules in our approach change the shape of a value object from its default shape to its most optimized one during the value object’s creation.

\(^3\)https://github.com/smarr/ReBench
\(^4\)https://bitbucket.org/krono/lamb-bench

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Figure 5: Referenced value object realisation. Accessing the second item \(2\) of the list \(l \leftarrow \text{Node/2[1, Node/2[2, Node/2[3, . . . ]]]}\) by two operations \texttt{head(tail(l))} results in two differently reified rest lists to be created. Note how the shapes of the rest lists differ.
Tracing JIT compilers as introduced by Mitchell [26] have seen implementations for Java [19], JavaScript [20], or Lua, to name a few. In the context of a JavaScript implementation, the SPUR project [5] provided a tracing JIT compiler for Microsoft’s Common Intermediate Language (CIL).

Tracing an interpreter that runs a program instead of tracing the program itself is the core idea of meta-tracing JIT compilers, pioneered in the DynamoRIO project [33]. PyPy [10, 30] is a meta-circular Python implementation that uses a meta-tracing JIT compiler. Provided through the RPython tool chain, other language implementations can benefit from a meta-tracing, e.g., Smalltalk [11], Haskell [35], PHP, or R. The meta-tracing JIT used in this work is provided by RPython, as well.

7. CONCLUSION AND FUTURE WORK

Our approach to just-in-time optimization of value classes provides very good initial results both for execution time and memory consumption for a small prototype implementation on selected micro-benchmarks. They are promising and motivate us to investigate the matter further.

Immediate next steps include the integration of our approach into existing programming language implementations. Here, languages that already have an implementation with a meta-tracing JIT compiler would be obvious candidates. Then, larger and more real-world benchmarks can be tackled.

Our aim is then to broaden the scope of our approach beyond value classes. We want to support objects that have identity as well as mutable objects. Yet, in the context of our optimization, these need more in-depth investigation.

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https://bitbucket.org/roy_andrew/rapydo
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